

Combining GLMs with GBMs for the Best of Your Pricing Models

Piotr Lebieź

ABOUT ME



Piotr Lebiedź

Guidewire
PricingCenter

- A seasoned pricing actuary, serving as Pricing Manager at Guidewire, driving adoption of a new pricing solution – Guidewire PricingCenter – across the globe.
- Specialized in empowering pricing leaders with the insights and tools necessary to navigate the ever-evolving pricing landscape.
- A passionate advocate for next-generation insurance pricing, committed to bridging actuarial expertise with cutting-edge technology to drive innovation across the industry.
- A university lecturer leading the actuarial path at Gdańsk University of Technology (Gdańsk, Poland).

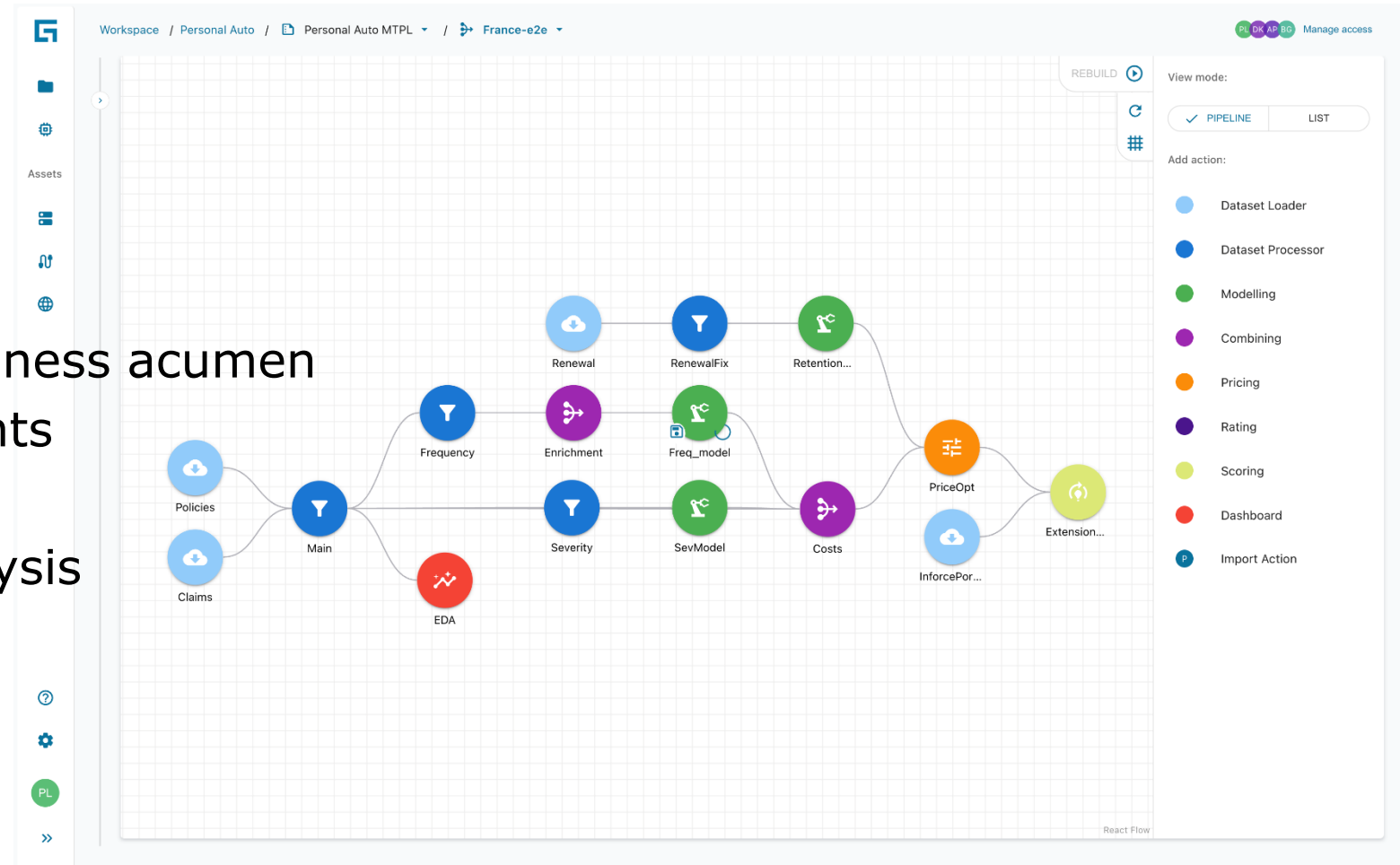
1. Quick intro to insurance pricing
2. GLM vs. GBM – comparison
 - i. definition and concept
 - ii. strengths and weaknesses
 - iii. typical applications in insurance pricing
3. GLM & GBM – hybrid approach
 - i. GBM helping in variable selection for GLM
 - ii. GBM as input to GLM
 - iii. GLM as input to GBM
 - iv. GLM residuals corrected by GBM
 - v. GLM and GBM ensembled
4. Key takeaways

1. **Quick intro to insurance pricing**
2. GLM vs. GBM – comparison
 - i. definition and concept
 - ii. strengths and weaknesses
 - iii. typical applications in insurance pricing
3. GLM & GBM – hybrid approach
 - i. GBM helping in variable selection for GLM
 - ii. GBM as input to GLM
 - iii. GLM as input to GBM
 - iv. GLM residuals corrected by GBM
 - v. GLM and GBM ensembled
4. Key takeaways

Insurance pricing aims to calculate fair price for particular risk transfer

Insurance pricing consists of:

- Data wrangling
- Data exploration
- Product understanding
- Risk modeling
- Expert judgement and business acumen
- Forward-looking adjustments
- Market analysis
- Competitor landscape analysis
- Price optimization
- Frequent price updates
- Constant monitoring
- And more...



1. Quick intro to insurance pricing
2. **GLM vs. GBM – comparison**
 - i. definition and concept
 - ii. strengths and weaknesses
 - iii. typical applications in insurance pricing
3. GLM & GBM – hybrid approach
 - i. GBM helping in variable selection for GLM
 - ii. GBM as input to GLM
 - iii. GLM as input to GBM
 - iv. GLM residuals corrected by GBM
 - v. GLM and GBM ensembled
4. Key takeaways

Definition and concept

GLM

- Full name: Generalized Linear Model
- Category: Linear estimator
- Domain: Identifying, quantifying, and combining independent univariate signals

GLM formula:

$$g(E(Y)) = X\beta$$

where:

g is a link function

$E(Y)$ is the expected value of the response variable Y

X is a matrix of predictor variables,

β is a vector of coefficients

GBM

- Full name: Gradient Boosting Machine
- Category: Tree-based estimator
- Domain: Identifying multivariate dependencies and microsegments
- Ensemble learning method: Boosting

GBM builds decision trees iteratively and corrects their combined errors on the way. Thanks to a gradient descent algorithm it minimizes the loss when adding new models.

Strengths and weaknesses

GLM

- + Well-known and market standard
- + Transparent formula once trained
- + Easily ingested by rating engines
- + Quick in real-time quoting
- Limited accuracy
- Assumes linearity
- Assumes feature independence
- Long time to build
- Subject to confirmation bias

GBM

- + Best-in-class accuracy
- + Natively catches non-linearity
- + Finds interactions and microsegments
- + Quick setup, little feature transformations
- Less-known and less-practiced
- Lack of transparency (black-box)
- Requires advanced engine for prod use
- Significant latency in real-time quoting
- Requires more data and is easier to overfit

Typical applications in insurance pricing

GLM

1. Risk models
2. Demand/elasticity models
3. Other models (churn, market price)

GBM

1. Residual risk models
2. Market price models
3. Other models (risk, demand, churn)

Feature	✓ ⚙ ^ 🔒	Coefficient	Relativity	Std. Error	p-value	Significance
INTERCEPT		-3.127	0.044	0.054	<.001	***
Features						
BONUS_MALUS						
BONUS_MALUS.BIN=[-inf;51.5)		0	1			
BONUS_MALUS.BIN=[51.5;68.5)		0.619	1.858	0.019	<.001	***
BONUS_MALUS.BIN=[68.5;72.5)		0.687	1.987	0.039	<.001	***
BONUS_MALUS.BIN=[72.5;76.5)		0.739	2.093	0.040	<.001	***
BONUS_MALUS.BIN=[76.5;85.5)		0.851	2.342	0.030	<.001	***
BONUS_MALUS.BIN=[85.5;95.5)		0.895	2.447	0.032	<.001	***
BONUS_MALUS.BIN=[95.5;inf)			5.160	0.028	<.001	***
DENSITY						

Estimator

Strategy

Gradient Boosting

Parameters

Num. Estimators *

200 × 300 × 400 × 500 ×

Maximum tree leaves *

100 ×

Minimum loss reduction *

0 ×

Subsample *

0.9 ×

Learning Rate *

0.01 × 0.001 × 0.0001 ×

Maximum tree depth *

-1 ×

Column Sample by Tree *

0.9 ×

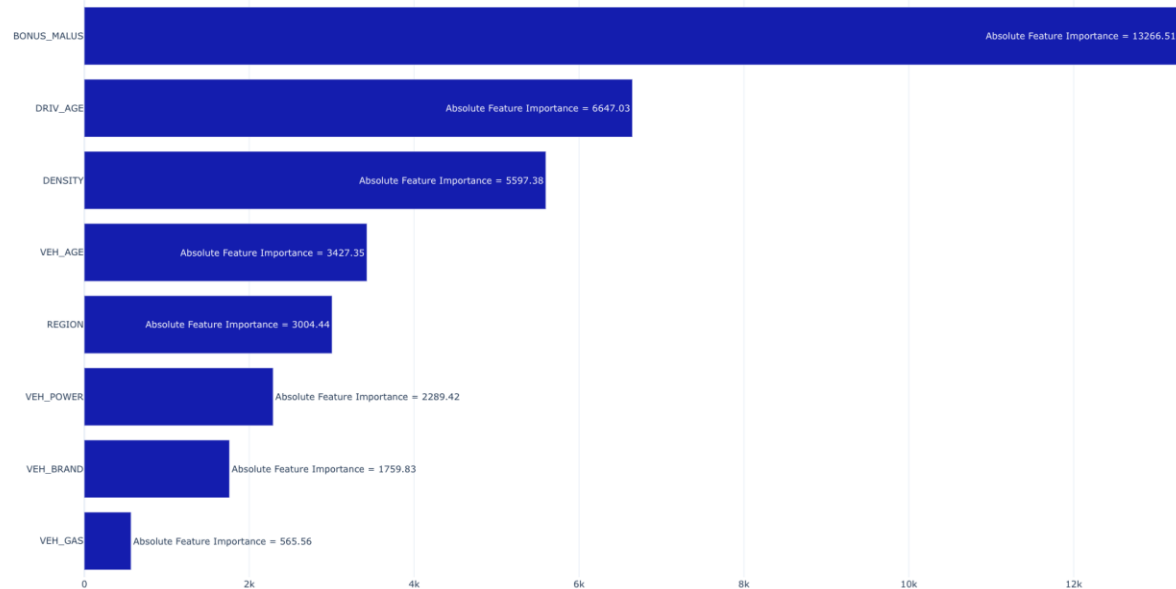
Frequency of subsample *

7 ×

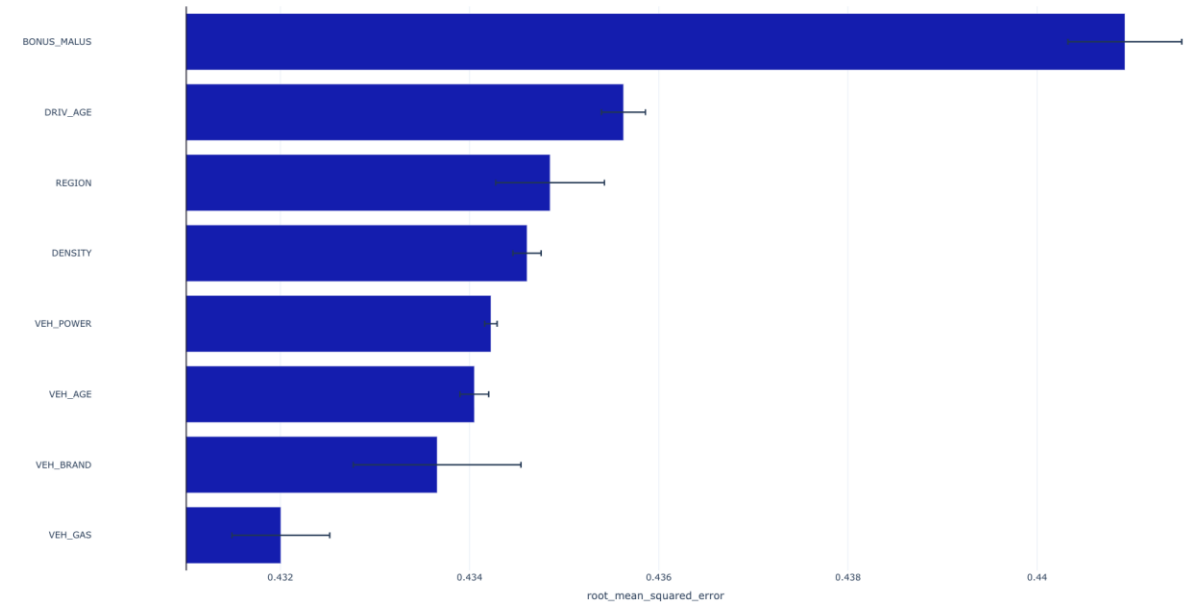
1. Quick intro to insurance pricing
2. GLM vs. GBM – comparison
 - i. definition and concept
 - ii. strengths and weaknesses
 - iii. typical applications in insurance pricing
3. **GLM & GBM – hybrid approach**
 - i. GBM helping in variable selection for GLM
 - ii. GBM as input to GLM
 - iii. GLM as input to GBM
 - iv. GLM residuals corrected by GBM
 - v. GLM and GBM ensembled
4. Key takeaways

GBM helping in variable selection for GLM

Tree-based feature importance

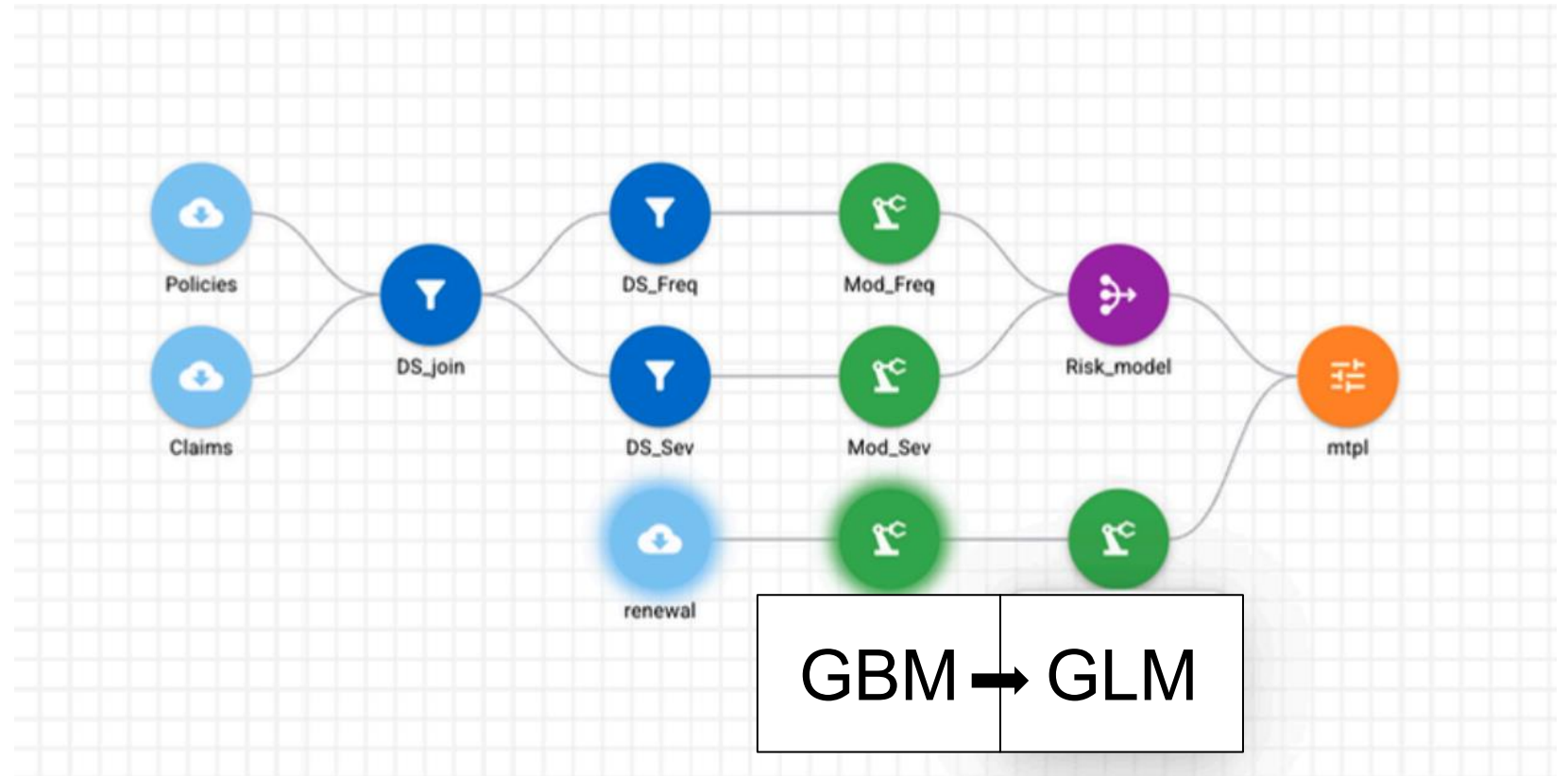


Model agnostic variable importance



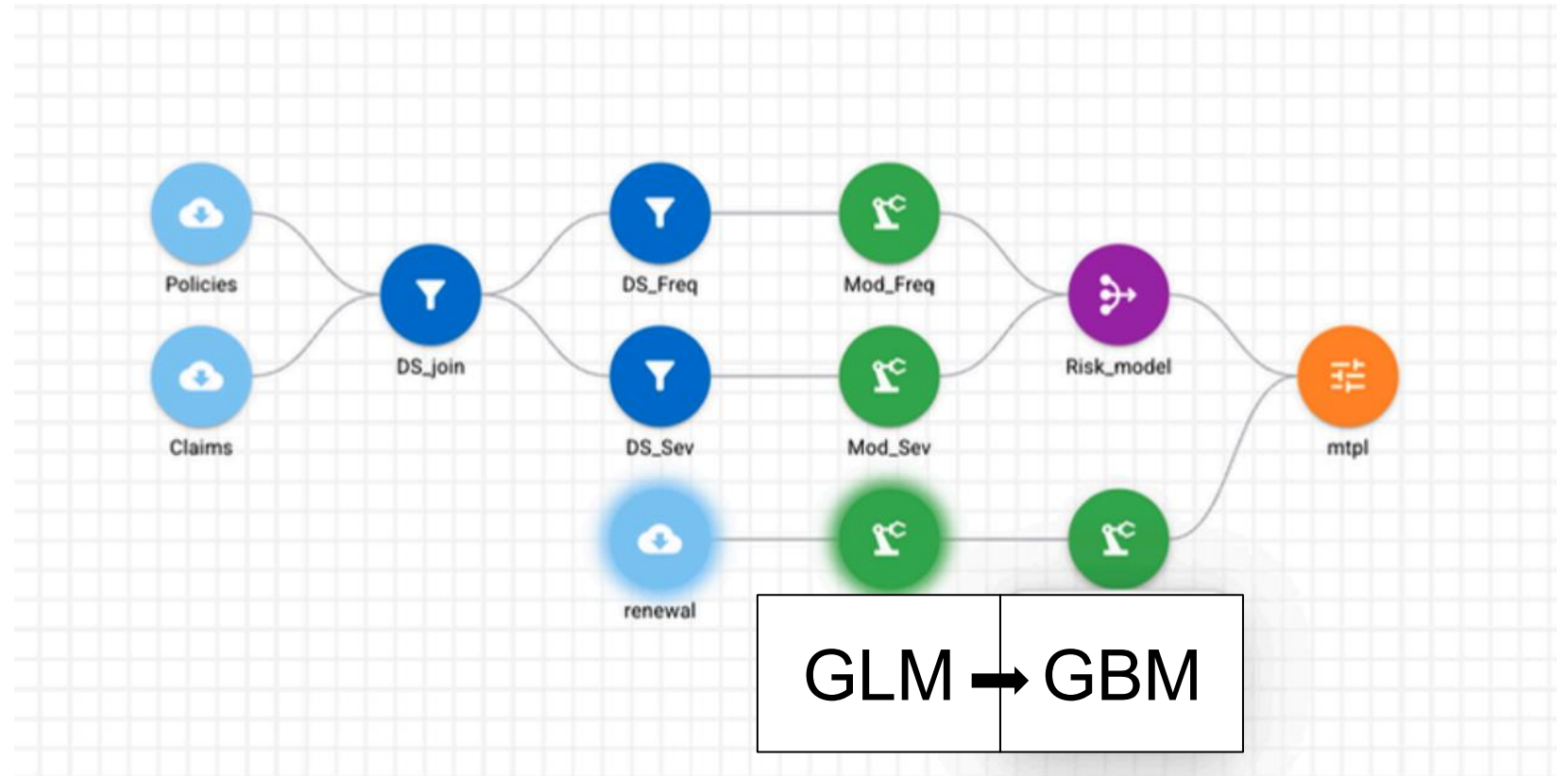
GBM as input to GLM

- Prediction = $GLM(GBM, x_1, x_2, x_3, \dots)$
- Controlled impact of GBM



GLM as input to GBM

- GBM's behavior controlled by adding predictions from GLM as input
- Allowing GBM to find more nuances, keeping the original target distribution



GLM residuals corrected by GBM

1. Fit GLM and get predictions y_{GLM}
2. Compute residuals: *actual value* – *prediction*
3. Train GBM on residuals (loss matching distribution of residuals) and get predictions \bar{y}_{GBM}
4. Update predictions: $y_{GLM} + \bar{y}_{GBM}$

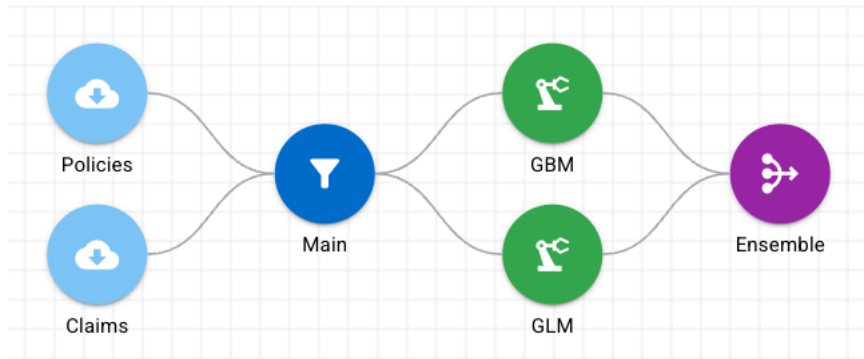


Combining ②

MTPL_actcost	Σ	(`Mod_Freq` + `GBM_residual`) * `Mod_Sev`	
MTPL_fix_cost	Σ	Lookup dataset	Cost_per_Area.xlsx (#491)
		Left on variable	AREA
		Right on variable	Area
		Lookup variable	Fixcost
		Not found value	15

GLM and GBM ensembled

1. Fit GLM and get predictions y_{GLM}
2. Fit GBM and get predictions y_{GBM}
3. Choose weights w between 0 and 1
4. Final predictions: $w \cdot y_{GLM} + (1 - w) \cdot y_{GBM}$



Combining ?

⋮	<input checked="" type="checkbox"/>	Weight	Σ	0.5
⋮	<input checked="" type="checkbox"/>	Ensembled_prediction	Σ	<code>`Ensemble.Weight` * `GLM` + (1 - `Ensemble.Weight`) * `GBM`</code>

1. Quick intro to insurance pricing
2. GLM vs. GBM – comparison
 - i. definition and concept
 - ii. strengths and weaknesses
 - iii. typical applications in insurance pricing
3. GLM & GBM – hybrid approach
 - i. GBM helping in variable selection for GLM
 - ii. GBM as input to GLM
 - iii. GLM as input to GBM
 - iv. GLM residuals corrected by GBM
 - v. GLM and GBM ensembled
4. **Key takeaways**

To summarise

- GLM and GBM are different tools in the actuarial toolkit
- GLM assesses individual signals well and is fully transparent
- GBM easily finds multivariate dependencies and microsegments but is 'black-box'
- GLM requires more actuarial expertise, while GBM requires data science rigour
- There is no 'better' or 'worse' between them
- They have different advantages and may serve different purposes
- One person or team can use both, either separately – for different cases, or...
- ... combine them for the same task to leverage the best of both
- Best-in-class pricing solutions are capable of building both kinds of models, applying a hybrid approach, and deploying them seamlessly to production

Thank you!

Please rate the conference via the survey-link you will receive per email.

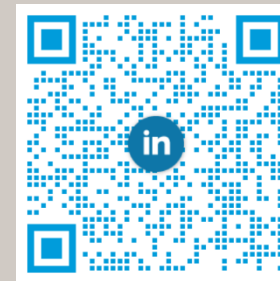
Visit our website



www.actuarial-academy.com

for more events.

Follow us on LinkedIn



www.linkedin.com/company/642904

for updates & actuarial fun.